

Journal of Data Science, Statistics, and Visualisation

August 2022, Volume II, Issue IV.

doi: 10.52933/jdssv.v2i4.43

## Compressed Sensing with a Jackknife, a Bootstrap, and Visualization

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## Abstract

This supplementary material provides the appendices, Appendices A and B.

*Keywords*: error estimation, visualization, medical imaging, magnetic resonance imaging, compressive sensing, compressive sampling.

## A. Supplementary jackknives and bootstraps

This appendix supplements Figures 2–5 of Section 3 with analogous figures for twenty cross-sectional slices through the head of the patient (Figures 2–5 of Section 3 are for slices 3 and 10).



Figure 1: Radially retained sampling — slice 1  $\,$ 



Figure 2: Radially retained sampling — slice 2  $\,$ 



Figure 3: Radially retained sampling — slice 3  $\,$ 



Figure 4: Radially retained sampling — slice 4  $\,$ 



Figure 5: Radially retained sampling — slice 5  $\,$ 



Figure 6: Radially retained sampling — slice 6



Figure 7: Radially retained sampling — slice 7  $\,$ 



Figure 8: Radially retained sampling — slice 8



Figure 9: Radially retained sampling — slice 9



Figure 10: Radially retained sampling — slice  $10\,$ 



Figure 11: Radially retained sampling — slice 11



Figure 12: Radially retained sampling — slice  $12\,$ 



Figure 13: Radially retained sampling — slice 13  $\,$ 



Figure 14: Radially retained sampling — slice 14



Figure 15: Radially retained sampling — slice 15



Figure 16: Radially retained sampling — slice 16



Figure 17: Radially retained sampling — slice 17  $\,$ 



Figure 18: Radially retained sampling — slice  $18\,$ 



Figure 19: Radially retained sampling — slice 19



Figure 20: Radially retained sampling — slice 20  $\,$ 



Figure 21: Horizontally retained sampling — slice 1  $\,$ 



Figure 22: Horizontally retained sampling — slice 2  $\,$ 



Figure 23: Horizontally retained sampling — slice 3  $\,$ 



Figure 24: Horizontally retained sampling — slice 4  $\,$ 



Figure 25: Horizontally retained sampling — slice 5  $\,$ 



Figure 26: Horizontally retained sampling — slice 6



Figure 27: Horizontally retained sampling — slice 7  $\,$ 



Figure 28: Horizontally retained sampling — slice 8



Figure 29: Horizontally retained sampling — slice 9  $\,$ 



Figure 30: Horizontally retained sampling — slice 10



Figure 31: Horizontally retained sampling — slice 11



Figure 32: Horizontally retained sampling — slice 12



Figure 33: Horizontally retained sampling — slice 13



Figure 34: Horizontally retained sampling — slice 14



Figure 35: Horizontally retained sampling — slice  $15\,$


Figure 36: Horizontally retained sampling — slice 16



Figure 37: Horizontally retained sampling — slice 17



Figure 38: Horizontally retained sampling — slice  $18\,$ 



Figure 39: Horizontally retained sampling — slice 19  $\,$ 



Figure 40: Horizontally retained sampling — slice  $20\,$ 



Figure 41: 2× radially retained sampling — slice 1



Figure 42: 2× radially retained sampling — slice 2



Figure 43: 2× radially retained sampling — slice 3



Figure 44: 2× radially retained sampling — slice 4



Figure 45: 2× radially retained sampling — slice 5



Figure 46: 2× radially retained sampling — slice 6



Figure 47: 2× radially retained sampling — slice 7



Figure 48: 2× radially retained sampling — slice 8



Figure 49: 2× radially retained sampling — slice 9



Figure 50: 2× radially retained sampling — slice 10



Figure 51: 2× radially retained sampling — slice 11



Figure 52: 2× radially retained sampling — slice 12



Figure 53: 2× radially retained sampling — slice 13



Figure 54: 2× radially retained sampling — slice 14



Figure 55:  $2\times$  radially retained sampling — slice 15



Figure 56: 2× radially retained sampling — slice 16



Figure 57: 2× radially retained sampling — slice 17



Figure 58: 2× radially retained sampling — slice 18



Figure 59: 2× radially retained sampling — slice 19



Figure 60:  $2\times$  radially retained sampling — slice 20



Figure 61: 2× horizontally retained sampling — slice 1



Figure 62: 2× horizontally retained sampling — slice 2



Figure 63: 2× horizontally retained sampling — slice 3



Figure 64: 2× horizontally retained sampling — slice 4



Figure 65: 2× horizontally retained sampling — slice 5



Figure 66: 2× horizontally retained sampling — slice 6



Figure 67: 2× horizontally retained sampling — slice 7



Figure 68: 2× horizontally retained sampling — slice 8



Figure 69: 2× horizontally retained sampling — slice 9



Figure 70: 2× horizontally retained sampling — slice 10



Figure 71: 2× horizontally retained sampling — slice 11


Figure 72: 2× horizontally retained sampling — slice 12



Figure 73: 2× horizontally retained sampling — slice 13



Figure 74: 2× horizontally retained sampling — slice 14



Figure 75: 2× horizontally retained sampling — slice 15



Figure 76: 2× horizontally retained sampling — slice 16



Figure 77: 2× horizontally retained sampling — slice 17



Figure 78: 2× horizontally retained sampling — slice 18



Figure 79: 2× horizontally retained sampling — slice 19



Figure 80: 2× horizontally retained sampling — slice 20

## B. Blurred errors over a threshold overlaid

For reference, this appendix displays the same errors over a threshold overlaid over the reconstruction as in Subsection 2.2, together with the blurred errors over a threshold overlaid over the reconstruction (blurring with a Gaussian convolutional kernel whose standard deviation is one pixel, as in Subsection 2.3). The labeling conventions ("lower," "upper," etc.) conform to those introduced in Section 3. The blurred errors certainly introduce less distracting noise than without blurring, yet the colors still appear really distracting.



Errors Over a Threshold Overlaid

Errors Over a Threshold Overlaid





Blurred Errors Over a Threshold Overlaid





Figure 81: Radially sampling (b) — upper plots display the upper slice; lower plots show the lower



Errors Over a Threshold Overlaid

Errors Over a Threshold Overlaid





Blurred Errors Over a Threshold Overlaid





Figure 82: Horizontally sampling (b) — upper plots show the upper slice; lower plots show the lower

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Journal of Data Science, Statistics, and Visualisation https://jdssv.org/ published by the International Association for Statistical Computing http://iasc-isi.org/

ISSN 2773-0689 August 2022, Volume II, Issue IV doi:10.52933/jdssv.v2i4.43

Submitted: 2021-04-19 Accepted: 2021-11-15